

## Tandem Queues:

The word ‘Tandem’ refers to an arrangement of objects in which the objects are lined up one behind the other, all facing in the same direction. In a Tandem queuing network there are multiple job classes, one after the other and an arriving customer undergoes each job class before leaving the system. In the discussed experiments, we consider a 3-stage tandem queuing network, with and without feedback. Each stage of service is assumed to behave as an  $M / M / 1$  queuing network.



The arrival rate of customers is  $\lambda$  and the service rate at node  $i$  is  $\mu_i$ . Let  $\rho_i = \frac{\lambda}{\mu_i}$ . Hence steady state measures are:

- $p(k_1, k_2, k_3) = P(k_i \text{ customers at node } i, i = 1, 2, 3) = \prod_{i=1}^3 \rho_i^{k_i} (1 - \rho_i)$
- Average number of customers at Node  $i$ :  $\frac{\rho_i}{1 - \rho_i}, i = 1, 2, 3$
- Average number of customers in the system:  $\sum_{i=1}^3 \frac{\rho_i}{1 - \rho_i}$
- Average number of customers in the queue of Node  $i$ :  $\frac{\rho_i^2}{1 - \rho_i}, i = 1, 2, 3$
- Total average number of customers in the queue:  $\sum_{i=1}^3 \frac{\rho_i^2}{1 - \rho_i}$
- Average waiting time of a customer in the queue of node  $i$ :  $\frac{\rho_i}{\mu_i - \lambda}$
- Average waiting time of a customer at node  $i$ :  $\frac{1}{\mu_i - \lambda}$
- Average waiting of a customer in the system:  $\sum_{i=1}^3 \frac{1}{\mu_i - \lambda}$
- Utilization of node  $i$ :  $\frac{\lambda}{\mu_i}$
- Throughput of node  $i$ :  $\lambda, i = 1, 2, 3$